

# Guide to the use and compilation of the MAS-SEOM code

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(Dated: April 2, 2020)

## I. SINGLE-LEVEL ANDERSON IMPURITY MODEL

The total Hamiltonian of a single-level AIM consists of three parts:

$$H_{\text{T}} = H_{\text{S}} + H_{\text{B}} + H_{\text{SB}}. \quad (1)$$

Each part is defined as ( $e = \hbar \equiv 1$  and  $k_{\text{B}} \equiv 1$ ):

$$\begin{aligned} H_{\text{S}} &= \epsilon_{\uparrow} \hat{n}_{\uparrow} + \epsilon_{\downarrow} \hat{n}_{\downarrow} + U \hat{n}_{\uparrow} \hat{n}_{\downarrow}, \\ H_{\text{B}} &= \sum_{\alpha k} \sum_s \epsilon_{\alpha k} \hat{d}_{\alpha k s}^{\dagger} \hat{d}_{\alpha k s}, \\ H_{\text{SB}} &= \sum_{\alpha} \sum_s \hat{c}_s^{\dagger} \hat{F}_{\alpha s} + \hat{F}_{\alpha s}^{\dagger} \hat{c}_s. \end{aligned} \quad (2)$$

As shown in Fig. 1, the impurity is coupled to two spin-unpolarized electron reservoirs ( $\alpha = L, R$ ). Both reservoirs have a spectral function of a Lorentz form, i.e.,

$$J_{\alpha}(\omega) \equiv \pi \sum_k |t_{\alpha k}|^2 \delta(\omega - \epsilon_{\alpha k}) = \frac{\Gamma_{\alpha}}{2} \frac{W_{\alpha}^2}{(\omega - \Omega_{\alpha})^2 + W_{\alpha}^2}, \quad (3)$$

## II. COMPILATION OF THE CODE

- The compiler is INTEL FORTRAN with MKL library.
- OpenMP parallelization is utilized.
- In Makefile, NAME: define the directory where the complied HEOM executable file (i.e., seom.x) will appear; e.g. NAME=/home/home/aa/seom.x
- "make clean" delete objects/\*.o, objmod/\*.o
- "make" obtains the MAS-SEOM executable file; can be of any name, e.g. seom

## III. INPUT FILE

- e1u  $\equiv$  energy of spin-up electron, e1d  $\equiv$  energy of spin-down electron, u1  $\equiv$  electron-electron coulomb interaction energy.
- dt  $\equiv$  timestep, ntime  $\equiv$  number of timestep
- ntraj  $\equiv$  number of trajectories, dref  $\equiv \lambda$
- nstate  $\equiv$  number of pseudo states
- Vlt1, Vlt2  $\equiv$  bias voltage
- nlead  $\equiv$  number of leads

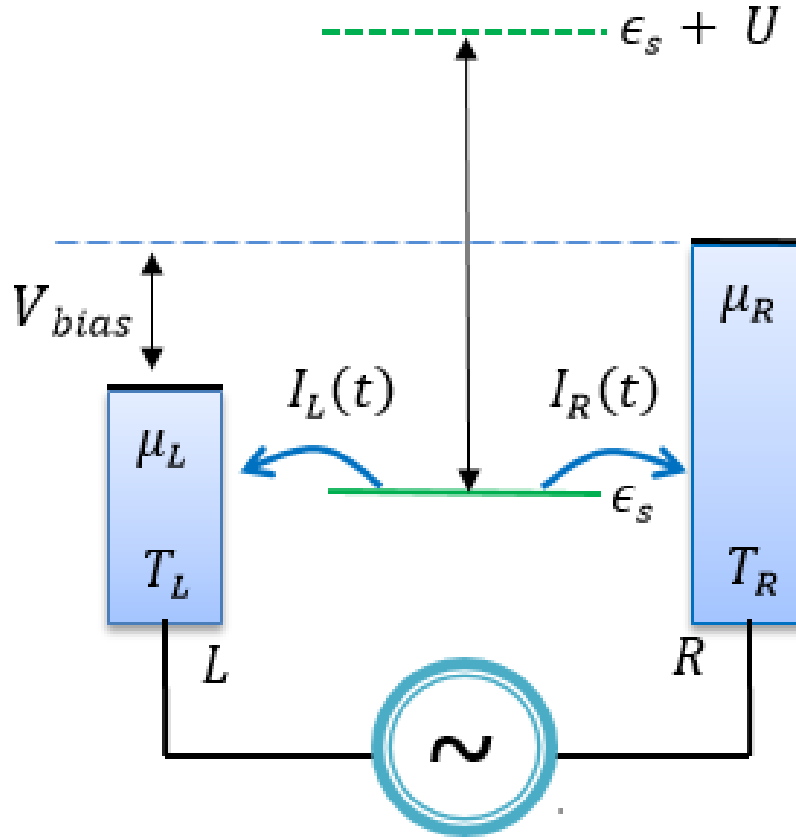


FIG. 1. Schematic diagram of a single-level impurity coupled with two electron reservoirs ( $\alpha = L, R$ ).  $\epsilon_s$  is the level energy for a spin- $s$  electron,  $U$  is the electron-electron Coulomb interaction energy, and  $\mu_\alpha$  and  $T_\alpha$  are the chemical potential and temperature of the  $\alpha$ -reservoir.  $I_\alpha(t)$  represents the current flow between the impurity and the  $\alpha$ -reservoir when a bias voltage  $V_{\text{bias}}$  is applied across the two reservoirs.

#### IV. OUTPUT FILES

run SEOM  $\rightarrow ./seom.x <input> output$

- population.dat, 2nd column  $\rightarrow$  population of spin-up, 3rd column  $\rightarrow$  population of spin-down
- 1current.dat, data for current using Eq.(36) [1], the 6th column is  $I_L$  while the 7th column is  $I_R$ .
- 2current.dat, data for current using Eq.(37) [1], the 2nd column is  $I_L$  while the 3rd column is  $I_R$ .

#### V. EXAMPLES

We have provided input files for the user to test the code

- by using the input file provided in "example-1" folder, user can generate the high temperature results of Fig.2,
- by using the input file provided in "example-2" folder, user can generate the low temperature results of Fig.2,
- by using the input file provided in "example-3" folder, user can generate Fig.3 results.

#### References

- [1] arXiv:1912.05271